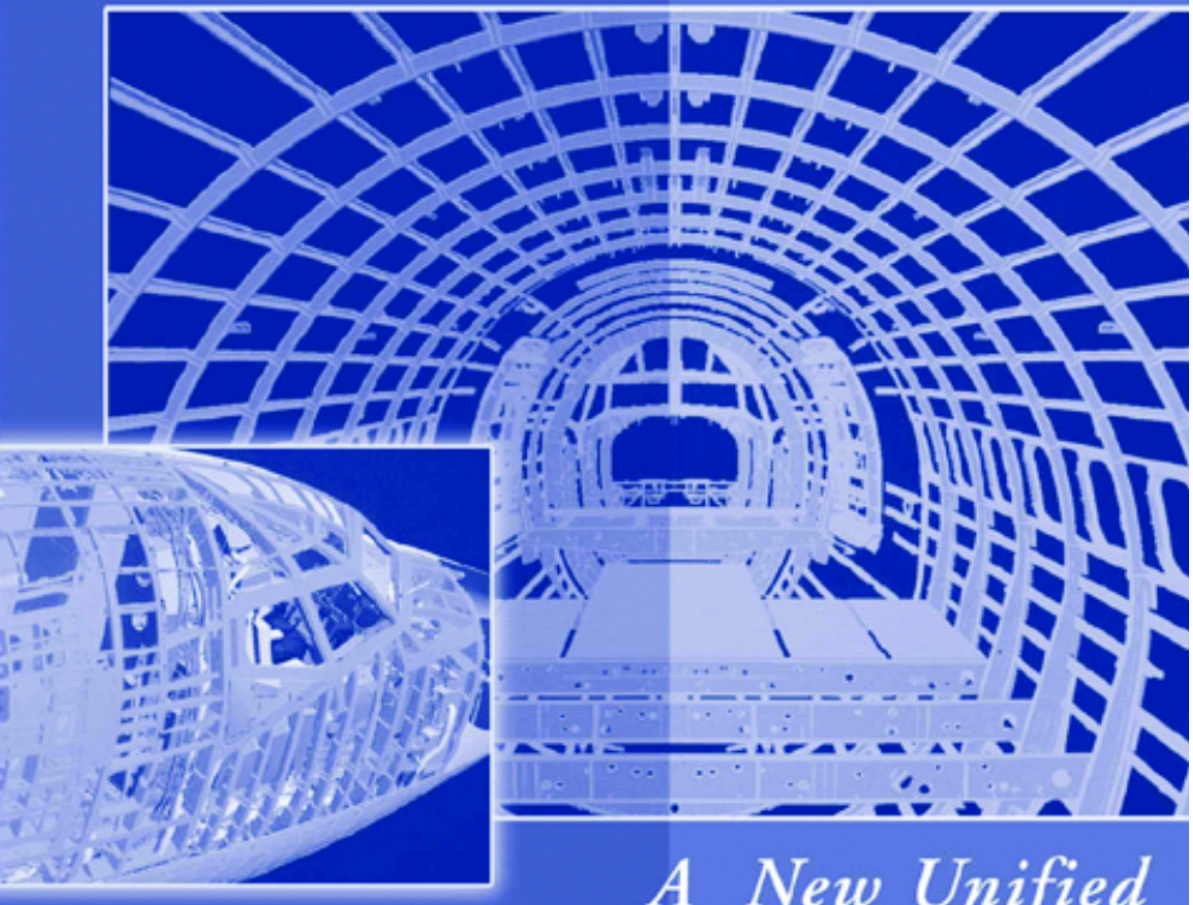
STRENGTH of MATERIALS



A New Unified Theory for the 21st Century

SURYA PATNAIK & DALE HOPKINS

Strength of Materials

Strength of Materials: A Unified Theory

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